One component bounded function

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One-component inner functions were first introduced by B. Cohn in [**C**] in connection with Carleson measures for model spaces. They are associated to some well-understood model spaces: indeed it is possible to provide an useful geometric characterization of Carleson measures for the model spaces corresponding to one-component inner functions. Some equivalent characterizations of one-component inner functions have been provided by A. Aleksandrov [**A**], by A. Nicolau and A. Reijonen [**NR**] and by R. Bessonov [**B**].

In this presentation, I will talk about the one-component bounded function. They were first introduced by A. Baranov, E. Fricain and J. Mashreghi in [**BFM**] where the authors studied the Carleson measure for the de Branges-Rovnyak spaces. After the definition the one-component bounded function, I will provide some equivalent descriptions, highlighting the differences with the inner case.

The results are part of a joint work with Prof. A. Nicolau.

References

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